

1-Assembly line balancing (Product)

* Definitions:

- Work element: It is the non-divisible part at final work breakdown
- Elemental time: It is the time of producing an element
- Work station time: It is the time at which element presents in the work station specified
- Total work content: It is the total of elemental times
- cycle time: It is time stations to work

* Laws:

Production rate = $\frac{1}{C}$ \rightarrow cycle time

$C = \frac{T}{N}$ \rightarrow Total time for production (Total work content)

$N_{min} = \frac{\sum_{i=1}^n t_i}{C}$ \rightarrow No. of products

\rightarrow Min no. of stations

$\bar{C} = \frac{\sum_{i=1}^n t_i}{n}$ \rightarrow Actual no. of stations $< C$

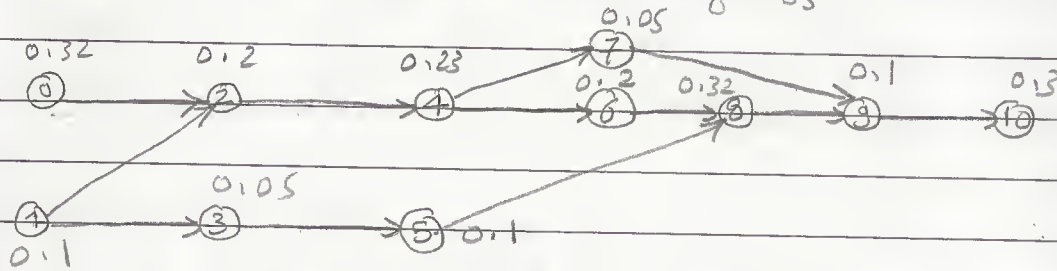
\rightarrow Actual cycle time

Balancing loss % = $\frac{C - \bar{C}}{C} \times 100\% = \frac{nC - \sum_{i=1}^n t_i}{nC} = 10.20\%$

Max. production rate = $\frac{1}{\text{time of workstation of min. time}}$

*Example:

It is required to balance the line, knowing that the cycle time is 0.55 hr (An O/P of 1.82 per hr). Determine the no. of stations & the balancing loss



* Using ranked positional weight

$(PW_i) = \sum_{j=1}^n t_j$; (n) all activities depending on 'i' and itself

$$PW_1 = 0.32 + 0.2 + 0.23 + 0.05 + 0.2 + 0.32 + 0.1 + 0.3 = 1.72 \text{ hr}$$

$$PW_2 = PW_1 - 0.32 + 0.05 + 0.1 + 0.1 = 1.65 \text{ hr}$$

$$PW_3 = PW_2 - 0.32 = 1.4 \text{ hr}$$

$$PW_4 = 0.05 + 0.1 + 0.32 + 0.1 + 0.3 = 0.87 \text{ hr}$$

$$PW_5 = PW_3 - 0.2 = 1.2 \text{ hr}$$

$$PW_6 = PW_5 - 0.05 = 0.82 \text{ hr}$$

$$PW_7 = 0.2 + 0.32 + 0.1 + 0.3 = 0.92 \text{ hr}$$

$$PW_8 = 0.05 + 0.1 + 0.3 = 0.45 \text{ hr}$$

$$PW_9 = 0.32 + 0.1 + 0.3 = 0.72 \text{ hr}$$

$$PW_{10} = 0.1 + 0.3 = 0.4 \text{ hr}$$

$$PW_{11} = 0.3 \text{ hr}$$

| | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | |
|------------------------|------|------|-----|------|------|------|------|------|------|------|------|-------|
| Element no. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | Total |
| Elemental time | 0.32 | 0.1 | 0.2 | 0.05 | 0.23 | 0.1 | 0.2 | 0.05 | 0.32 | 0.1 | 0.3 | 1.97 |
| PW | 1.72 | 1.65 | 1.4 | 0.87 | 1.2 | 0.82 | 0.92 | 0.45 | 0.72 | 0.4 | 0.3 | |
| Immediate Predecessors | — | — | 0,1 | 1 | 2 | 3 | 4 | 4 | 5,6 | 8 | 9 | |

$$n_{min} = \frac{\sum_{i=1}^{10} t_i}{C} = \frac{1.97}{0.55} = 3.58 \rightarrow 4$$

PW decreases

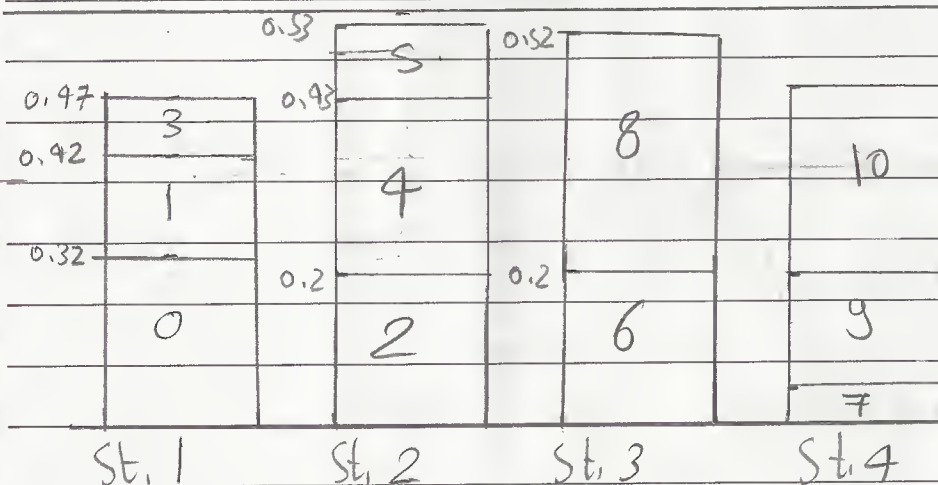
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| Work station | Element | PW | Immediate predecessor | Elemental time (t _e) | Cumulative station time (C) | Unassigned station time (C-x) |
|--------------|---------|------|-----------------------|----------------------------------|-----------------------------|-------------------------------|
| 1 | 0 | 1.72 | — | 0.32 | 0.32 | 0.23 |
| | 1 | 1.65 | — | 0.1 | 0.42 | 0.13 |
| | 3 | 0.97 | 1 | 0.05 | 0.47 | 0.08 |
| 2 | 2 | 1.4 | 0,1 | 0.2 | 0.2 | 0.35 |
| | 4 | 1.2 | 2 | 0.23 | 0.43 | 0.12 |
| | 5 | 0.82 | 3 | 0.1 | 0.53 | 0.02 |
| 3 | 6 | 0.92 | 4 | 0.2 | 0.2 | 0.32 |
| | 8 | 0.72 | 5,6 | 0.32 | 0.52 | 0.03 |
| 4 | 7 | 0.45 | 4 | 0.05 | 0.05 | 0.5 |
| | 9 | 0.4 | 8 | 0.1 | 0.15 | 0.4 |
| | 10 | 0.3 | 9 | 0.3 | 0.45 | 0.1 |

Balancing of work stations

0.55



$$\text{Balancing loss} = \frac{nC - \sum_{i=1}^n t_i}{nC} = 1 - \frac{1.97}{4 \times 0.55} \times 100 = 10.45\%$$

Subject.

2. Group technology (Cellular M.S.)

* Component operation matrix:

| Component | Operation (1) | Operation (2) | ... | Operation (n) |
|-----------|---------------|---------------|-----|---------------|
| 1 | x_1 | | | |
| 2 | x_2 | | | |
| ... | | | | |
| n | x_n | | | z_n |

↑ Component no. ↑ Mic no.

— Ranked order cluster (R.O.C.): Max. no. of m/c's in one cell

| Comp. M/C | 1 | 2 | - | - | - | n | Binary value |
|--------------|--|---|---|---|---|---|--------------|
| 1 | Fill with (1) in its place → Repeated not filled twice | | | | | | |
| 2 | | | | | | | |
| 3 | | | | | | | |
| 1 | | | | | | | |
| 1 | | | | | | | |
| 1 | | | | | | | |
| 1 | | | | | | | |
| 14 | | | | | | | |
| ↑ | | | | | | | |

Biggest
no. in component operation matrix

1. Calculate binary values of each row: $B.V_i = \sum_{j=1}^n x_{ij} \times 2^{n-j}$
2. Arrange rows descendingly according to their B.V.s
3. Construct a new (C.O.M)
4. Calculate binary values of each column: $B.V_j = \sum_{i=1}^n x_{ij} \times 2^{n-i}$
5. Arrange columns descendingly acc. to their B.V.s
6. Repeat the previous steps till both rows & columns are arranged descendingly together

* Example:

| Component | Operation (1) | Operation (2) | Operation (3) | Operation (4) |
|-----------|---------------|---------------|---------------|---------------|
| 1 | 2 | 3 | 8 | |
| 2 | 2 | 6 | 8 | 9 |
| 3 | 9 | 8 | 4 | 8 |
| 4 | 3 | 5 | | |
| 5 | 1 | 5 | | |
| 6 | 7 | 4 | 7 | |
| 7 | 1 | 5 | | |
| 8 | 4 | 7 | (10) | |
| 9 | 5 | 3 | 1 | |

- R.O.C.

| | (256) | (128) | (64) | (32) | (16) | (8) | (4) | (2) | (1) | |
|-------|-------|-------|------|------|------|-----|-----|-----|-----|------|
| Comp. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | B.V. |
| 1 | | | | | 1 | | 1 | | 1 | 21 |
| 2 | 1 | 1 | | | | | | | | 384 |
| 3 | | | | 1 | | | | | 1 | 33 |
| 4 | | | 1 | | | 1 | | 1 | 1 | 74 |
| 5 | | | | 1 | 1 | | 1 | | 1 | 53 |
| 6 | | 1 | | | | | | | | 128 |
| 7 | | | | | | 1 | | 1 | | 10 |
| 8 | 1 | 1 | 1 | | | | | | | 448 |
| 9 | 1 | 1 | 1 | | | | | | | 448 |
| 10 | | | | | | | | 1 | | 2 |

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K&A
ANGLISA

| mic \ comp. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | B.V. |
|-------------|-----|-----|-----|----|-----|----|----|----|----|------|
| (12) 8 | 1 | 1 | 1 | | | | | | | 448 |
| (25) 9 | 1 | 1 | 1 | | | | | | | 448 |
| (128) 2 | 1 | 1 | | | | | | | | 384 |
| (64) 6 | | 1 | | | | | | | | 1128 |
| (32) 4 | | | 1 | | | 1 | | 1 | | 74 |
| (16) 5 | | | | 1 | 1 | | 1 | | 1 | 53 |
| (8) 3 | | | | 1 | | | | | 1 | 33 |
| (4) 1 | | | | | 1 | | 1 | | 1 | 21 |
| (2) 7 | | | | | | 1 | | 1 | | 10 |
| (1) 10 | | | | | | | | 1 | | 2 |
| B.V. | 836 | 960 | 800 | 24 | 210 | 34 | 20 | 35 | 28 | |

| | (256) | (128) | (64) | (32) | (16) | (8) | (4) | (2) | (1) | |
|-------------|-------|-------|------|------|------|-----|-----|-----|-----|------|
| mic \ comp. | 2 | 1 | 3 | 8 | 6 | 4 | 9 | 5 | 7 | B.V. |
| 8 | 1 | 1 | 1 | | 1 | | | | 1 | 448 |
| 9 | 1 | 1 | 1 | | | | | | | 448 |
| 2 | 1 | 1 | | | | | | | | 384 |
| 6 | 1 | | | | | | | | | 256 |
| 4 | | | 1 | 1 | 1 | | | | 1 | 112 |
| 5 | | | | | | 1 | 1 | 1 | 1 | 15 |
| 3 | | | | | | 1 | 1 | 1 | 1 | 12 |
| 1 | | | | | | | 1 | 1 | 1 | 7 |
| 7 | | | | 1 | 1 | | | | | 48 |
| 10 | | | | 1 | | | | | | 32 |
| B.V. | 960 | 936 | 800 | 35 | 34 | 28 | 24 | 20 | 20 | |

Date.

Subject.

| Comp. M/C | 2 | 1 | 3 | 8 | 6 | 4 | 9 | 5 | 7 | B.V. |
|--------------|-----|-----|-----|----|----|---|---|---|---|------|
| (S12) 8 | 1 | 1 | 1 | | | | | | | 448 |
| (256) 9 | 1 | 1 | 1 | | | | | | | 448 |
| (128) 2 | 1 | 1 | | | | | | | | 384 |
| (64) 6 | 1 | | | | | | | | | 256 |
| (32) 4 | | | 1 | 1 | 1 | | | | | 112 |
| (16) 7 | | | | 1 | 1 | | | | | 48 |
| (8) 10 | | | | 1 | | | | | | 32 |
| (4) 5 | | | | | | 1 | 1 | 1 | 1 | 15 |
| (2) 3 | | | | | | 1 | 1 | | | 12 |
| (1) 1 | | | | | | | 1 | 1 | 1 | 7 |
| B.V. | 960 | 896 | 800 | 56 | 48 | 6 | 7 | 5 | 5 | |

| Comp. M/C | 2 | 1 | 3 | 8 | 6 | 9 | 4 | 5 | 7 | B.V. |
|--------------|-----|-----|-----|----|----|---|---|---|---|------|
| 8 | 1 | 1 | 1 | | | | | | | 448 |
| 9 | 1 | 1 | 1 | | | | | | | 448 |
| 2 | 1 | 1 | | | | | | | | 384 |
| 6 | 1 | | | | | | | | | 256 |
| 4 | | | 1 | 1 | 1 | | | | | 112 |
| 7 | | | | 1 | 1 | | | | | 48 |
| 10 | | | | 1 | | | | | | 32 |
| 5 | | | | | | 1 | 1 | 1 | 1 | 15 |
| 3 | | | | | | 1 | 1 | | | 12 |
| 1 | | | | | | 1 | | 1 | 1 | 7 |
| B.V. | 960 | 896 | 800 | 56 | 48 | 6 | 7 | 5 | 5 | |

For component (3) semi operations are done in both cells
or one other m/c is used

| Cell (1) | Cell (2) | Cell (3) |
|----------------------|------------------|------------------------|
| M/C 8 9 2 6 | M/C 4 7 10 | M/C 5 3 1 |
| Comp. 2 1 3 | Comp. 8 6 | Comp. 9 4 5 7 |

* Hollier's Algorithm: Min. distance from/to

1. Develop From/To chart from past routing data

2. Determine F & T sums

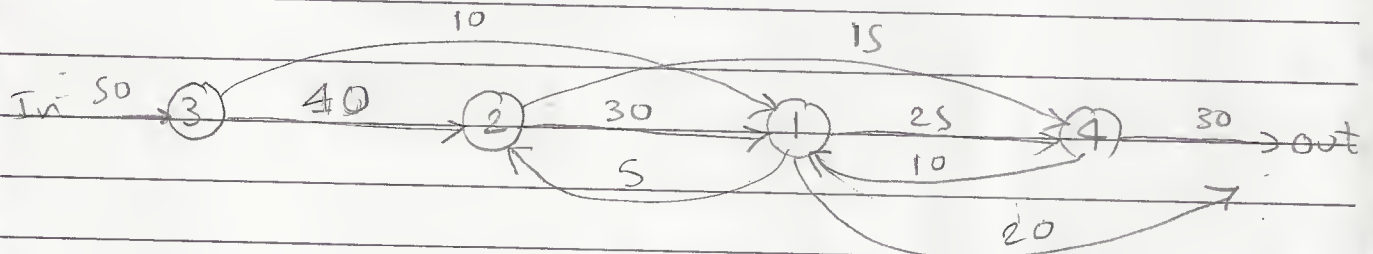
3. Assign mics to cells base on min F or T

4. Draw routing diagram & check to add some parts

Example:

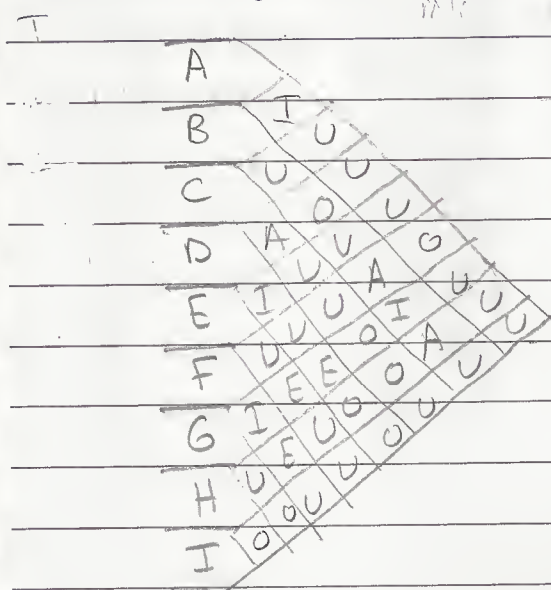
| From \ To | 1 | 2 | 3 | 4 | Sum |
|-----------|----|----|----|----|----------|
| 1 | 0 | 5 | 0 | 25 | 30 30 25 |
| 2 | 30 | 0 | 0 | 15 | 45 45 |
| 3 | 10 | 40 | 0 | 0 | 50 |
| 4 | 10 | 0 | 0 | 0 | 10 10 10 |
| Sum | 50 | 45 | 40 | 40 | |
| | 40 | 5 | 40 | | |
| | 10 | | | 25 | |

(3) → (2) → (1) or (4)

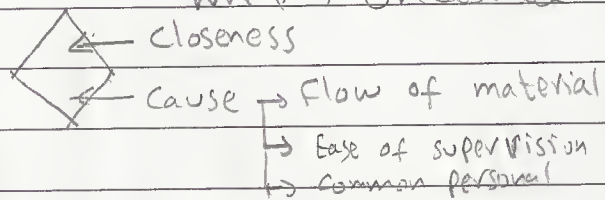


3 Facility Planning layout (process)

* Activity relationship chart:



- ≡ (A) Absolutely necessary
- ≡ (E) Especially necessary
- = (I) Important
- (O) Ordinary
- (U) Unimportant
- mm (X) Undesired



* Activity relationship diagram:

A

E

I

X

B — F

D — G

A — B

C — D

E — G

B — G

B — H

F — H

D — E

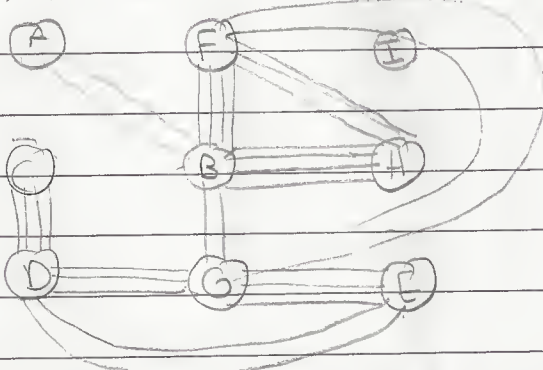
F — G

High effective → low quantity

Low effective → High quantity

⇒ (O or U) are not considered

9 → 3x3 → square as it is possible



| | | |
|---|---|---|
| A | F | I |
| C | B | H |
| D | G | E |

Block layout

Activity relationship diagram

Repeat according to no. of repetitions

Date.

* From-To chart from sequence matrix:

| Product | Sequence | Monthly production volume | Bulk factor | No. of unit loads |
|---------|--|---------------------------|-------------|-----------------------|
| 1 | ^{20 20 20 20 20} A B C D E F | 800 | 40 | $20 = \frac{800}{40}$ |
| 2 | A B D E D C F | 1000 | 40 | 25 |
| 3 | A B C F | 600 | 20 | 30 |
| 4 | A B C F B C F | 2000 | 20 | 100 |
| 5 | A C E F | 1500 | 20 | 75 |
| 6 | A B C D E F | 400 | 20 | 20 |
| 7 | A B C B D B E F | 2500 | 50 | 50 |
| 8 | A B D E C B F | 2000 | 50 | 40 |
| 9 | A B C D F | 800 | 40 | 20 |
| 10 | A B D E F | 1000 | 5 | 20 |

Fill the unit * Flow matrix:

| From \ To | A | B | C | D | E | F | Total |
|-----------|---|---|----------------------------|---------------------|-----------------------|----------------------|-------|
| A | 0 | 20, 25, 30 100, 20, 50 40, 20, 20 | 75 | | | | |
| B | | 0 | 20, 100, 100 20, 50, 20 | 25, 50, 40 20, 1 | 30, 50 | 50, 40 | |
| C | | 50, 40 | 0 | 20, 20, 20 | 100, 75 | 25, 100 | |
| D | | 50, 1 | 25 | 0 | 20, 25, 20 40, 120 | 20 | |
| E | | 100, 50 | 40, 1 | 25, 1 | 0 | 20, 30, 75 20, 20 | |
| F | | | | | | 0 | |
| Total | | | | | | | |

| From \ To | A | B | C | D | E | F | Total |
|-----------|---|-----|-----|-----|-----|-----|-------|
| A | 0 | 325 | 75 | 0 | 0 | 0 | 400 |
| B | 0 | 0 | 310 | 135 | 80 | 90 | 615 |
| C | 0 | 90 | 0 | 60 | 175 | 18 | 450 |
| D | 0 | 50 | 25 | 0 | 125 | 20 | 220 |
| E | 0 | 150 | 40 | 25 | 0 | 165 | 380 |
| F | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Total | 0 | 615 | 450 | 220 | 380 | 400 | 2065 |

4. Total material handling Cost (TMHC)

Example:

| Product | Prod ⁿ Vol. | Bulk factor | Sequence | Man. quantity |
|---------|------------------------|-------------|----------------------|---------------|
| 1 | 8000 | 200 | 11 22 44 66 55 88 | 40 |
| 2 | 4000 | 100 | 11 33 55 77 66 88 | 40 |
| 3 | 5000 | 100 | 11 44 33 66 77 33 88 | 50 |
| 4 | 600 | 20 | 11 22 33 55 22 88 | 30 |
| 5 | 800 | 50 | 11 55 44 22 66 88 | 16 |
| 6 | 5000 | 50 | 11 44 55 66 77 88 | ✓ |
| 7 | 4000 | 100 | 11 55 66 33 44 66 88 | 40 |
| 8 | 1000 | 50 | 11 22 33 66 55 66 88 | 20 |

For product 1, after completing its process at (44), it is split to 2 paths:

- 1- 60% of the production volume continues processing through the given sequence with a bulk factor of 50
- 2- 40% of the production volume continues through the following sequence: (44 77 33 44 55 77 88) with a bulk factor of 20

| | | | | | |
|-----|----|------|----|-------------------------|-----|
| * 1 | 6a | 3000 | 50 | 11 44 55 66 77 88 | 60 |
| | 6b | 2000 | 20 | 11 44 77 33 44 55 77 88 | 100 |

1- Flow matrix

| From \ To | 11 | 22 | 33 | 44 | 55 | 66 | 77 | 88 | Total |
|-----------|----|-----|-----|-----|-----|-----|-----|-----|-------|
| 11 | 0 | 90 | 40 | 210 | 56 | 0 | 0 | 0 | 396 |
| 22 | 0 | 0 | 50 | 40 | 0 | 16 | 0 | 0 | 106 |
| 33 | 0 | 0 | 0 | 140 | 70 | 50 | 0 | 50 | 310 |
| 44 | 0 | 16 | 50 | 0 | 60 | 80 | 0 | 0 | 206 |
| 55 | 0 | 30 | 0 | 16 | 0 | 130 | 140 | 0 | 316 |
| 66 | 0 | 0 | 40 | 0 | 60 | 0 | 110 | 116 | 326 |
| 77 | 0 | 0 | 180 | 0 | 0 | 40 | 0 | 160 | 380 |
| 88 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Total | 0 | 136 | 330 | 406 | 246 | 316 | 250 | 326 | 2010 |

Subject: 2010

2. Assumed layout;

| | | | |
|----|----|----|----|
| 11 | 55 | 22 | 77 |
| 33 | 88 | 66 | 44 |

$$TMHC = \sum_{i=1}^n \sum_{j=1}^n f_{ij} d[a(i), a(j)] C_{ij} ; \text{ For non-symmetric matrix}$$

$$TMHC = \frac{1}{2} \sum_{i=1}^n \sum_{j=1}^n f_{ij} d[a(i), a(j)] C_{ij} ; \text{ For symmetric matrix}$$

$$\begin{matrix} x' & y' \\ x'' & y'' \end{matrix} \quad \frac{x' + x''}{2} = x$$

3 - Cost matrix;

Not stated \rightarrow (11)

| From \ To | 11 | 22 | 33 | 44 | 55 | 66 | 77 | 88 |
|-----------|----|----|----|----|----|----|----|----|
| 11 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 22 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 |
| 33 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 |
| 44 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 |
| 55 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 |
| 66 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 1 |
| 77 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 |
| 88 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |

4. Distance matrix;

Distance \rightarrow Linear (Line from point to point)
 \rightarrow Rectilinear (x,y) \rightarrow Used
 \rightarrow Actual

| From \ To | 11 | 22 | 33 | 44 | 55 | 66 | 77 | 88 |
|-----------|----|----|----|----|----|----|----|----|
| 11 | 0 | 2 | 1 | 4 | 1 | 3 | 3 | 2 |
| 22 | 2 | 0 | 3 | 2 | 1 | 1 | 1 | 2 |
| 33 | 1 | 3 | 0 | 3 | 2 | 1 | 1 | 2 |
| 44 | 4 | 2 | 3 | 0 | 3 | 1 | 1 | 2 |
| 55 | 1 | 1 | 2 | 3 | 0 | 2 | 1 | 2 |
| 66 | 3 | 1 | 1 | 1 | 2 | 0 | 2 | 1 |
| 77 | 3 | 1 | 1 | 1 | 1 | 2 | 0 | 3 |
| 88 | 2 | 2 | 2 | 2 | 2 | 1 | 3 | 0 |

4. MHTC matrix:

| From \ To | 11 | 22 | 33 | 44 | 55 | 66 | 77 | 88 | Total |
|-----------|----|-----|-----|------|-----|-----|-----|-----|-------|
| 11 | 0 | 180 | 40 | 840 | 56 | 0 | 0 | 0 | 1116 |
| 22 | 0 | 0 | 150 | 80 | 0 | 16 | 0 | 0 | 246 |
| 33 | 0 | 0 | 0 | 420 | 140 | 50 | 0 | 50 | 660 |
| 44 | 0 | 32 | 150 | 0 | 180 | 80 | 0 | 0 | 442 |
| 55 | 0 | 30 | 0 | 48 | 0 | 260 | 140 | 0 | 478 |
| 66 | 0 | 0 | 40 | 0 | 120 | 0 | 220 | 116 | 496 |
| 77 | 0 | 0 | 150 | 0 | 0 | 80 | 0 | 320 | 550 |
| 88 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Total | 0 | 242 | 480 | 1388 | 496 | 496 | 360 | 486 | |

$$MHTC = 3988 + 3948 = 7936 \text{ unit of cost}$$